Abstract Algebra: The Theory of Groups

Syllabus 2014

Aim of the course: To get students to understand group theory without going too much into the rigor of proofs but rather to develop their intuition regarding the topic.

My reference book: Contemporary Abstract Algebra, 7th Edition, J. Gallian (there are many more books!)

Topics of study:

- 1. "What is a group?"
- 2. "What is the reason for the existence of groups?"
- 3. "How does its existence make me happy?"

"What is a group?"- Definition of a group, examples of groups, introduction to symmetry, properties of groups, history of groups (very briefly!).

"What is the reason for the existence of groups?"- A few applications (just mere introduction), symmetry, cyclic groups, permutation groups.

"How does its existence make me happy?"- Finite groups, subgroups and their tests, homomorphism (very briefly), isomorphism, cosets, Lagrange's theorem, external direct product, factor groups, Fundamental theorem of finite abelian groups (not too involved).

The catch of the course: To understand the power and beauty of mathematics and life in general, and how one can really know all there is to know by asking the questions to themselves!

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